Czech Technical University in Prague Faculty of Information Technology Department of Theoretical Computer Science



DISSERTATION THESIS TITLE

by

YOUR NAME

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Supervisor:

prof. PETER SUPERVISOR, Ph.D. Department of Theoretical Computer Science Faculty of Information Technology Czech Technical University in Prague Thákurova 9 160 00 Prague 6 Czech Republic

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Abstract and contributions

This dissertation thesis deals with \ldots

In particular, the main contributions of the dissertation thesis are as follows:

- 1. Design of a methodology of a ...
- 2. ...
- 3. ...

Keywords:

keyword1, keyword2, keyword3, keyword4, keyword5.

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Dedication

. . .

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Abbreviations

Number Sets

- \mathbb{N} Natural numbers set
- \mathbb{N}_0 Natural numbers set $\cup \{0\}$
- \mathbb{Z} Integer numbers set
- \mathbb{Z}_m Least nonzero residue number set with a module of m
- \mathbb{S}_m Symmetric residue number set with a module of m
- \mathbb{Q} Rational numbers set
- \mathbb{F}_t Floating point numbers set with a precision of t
- \mathbb{R} Real numbers set

Common Mathematical Functions and Operators

10_2	Numbers' radices are designated with a subscript
b	Vector b
b_i	the i^{th} element of vector b
$ \mathbf{b} $	Norm of vector \mathbf{b}
$\dim \mathbf{b}$	Dimension of vector \mathbf{b}
Α	Matrix \mathbf{A}
$a_{i,j}$	Element of matrix A at the i^{th} row, and the j^{th} column
\mathbf{A}^{-1}	Inverse matrix to matrix \mathbf{A}
\mathbf{A}^T	Transposed matrix to matrix \mathbf{A}
$ \mathbf{A} $	Norm of matrix \mathbf{A}
$\operatorname{cond} \mathbf{A}$	Condition number of matrix \mathbf{A}
$\mathrm{rank}\mathbf{A}$	Rank of matrix \mathbf{A} — how many independent rows/columns it has
$\max\left\{a,b\right\}$	Maximum of a and b , a when $a \ge b$, b when $a < b$
$\min\left\{a,b\right\}$	Minimum of a and b, a when $a \leq b$, b when $a > b$
O(x)	The big O notation
$\Theta(x)$	The big Θ notation

Mathematical Terminology

Miscellaneous Abbreviations

FPU Floating Point Unit

•••• ····

CHAPTER

Introduction

In this chapter, we...

1.1 Motivation

...[1] ...

1.2 Problem Statement

Brief description of the topic of the dissertation thesis. A complete explanation of the topic shall be described within chapter 2 at page 3.

1.3 Related Work/Previous Results

1.4 Goals of the Dissertation Thesis

- 1. ...
- 2. ...
- 3. . . .

1.5 Structure of the Dissertation Thesis

The thesis is organized into ... chapters as follows:

1. *Introduction*: Describes the motivation behind our efforts together with our goals. There is also a list of contributions of this dissertation thesis.

1. INTRODUCTION

- 2. *Background and State-of-the-Art*: Introduces the reader to the necessary theoretical background and surveys the current state-of-the-art.
- 3. Overview of Our Approach: ...
- 4. Main Results: ...
- 5. *Conclusions*: Summarizes the results of our research, suggests possible topics for further research, and concludes the thesis.

CHAPTER 2

Background and State-of-the-Art

. . .

- 2.1 Theoretical Background
- 2.2 Previous Results and Related Work

CHAPTER **3**

Overview of Our Approach

The sample Fig. 3.1 shows ...

0	0.25	C.U	0.75	1	1.25	1.5	1.75	7	2.5	$\tilde{\omega}$	3.5	4	Ś	Ň	9 7
L			1.1								-				
			1 1						1		1				I I

Figure 3.1: Distribution of the floating point numbers. This figure shows a distribution of a sample floating point number set with a precision t = 3, and $e_{min} = -1$ and $e_{max} = 3$.

There are two basic floating point data types , as defined by the IEEE 754-2008 [1] standard, are shown in Tab. 3.1.

	$\mathbf{Sign} \ [b]$	Exponent [b]	Mantissa [b]	Prec. [dig]	Total [b]
binary32	1	8	24	8	32
binary64	1	11	53	16	64

Table 3.1: Basic floating point data types.



Main Results

- 4.1 Main Result 1
- 4.2 Main Result 2

4.3 Main Result 3

Theorem 4.3.1. Some theorem...

Proof. Its proof...

Corollary 4.3.2. The corollary is...

4.4 Discussion

4.5 Summary

CHAPTER 5

Conclusions

5.1 Summary

5.2 Contributions of the Dissertation Thesis

5.3 Future Work

The author of the dissertation thesis suggests to explore the following:

- It would be interesting to ...
- $\circ~{\rm Consider}$. . .
- The implementation of our methodology could be further improved ...
- $\circ\,$ Apply the \ldots

o ...

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Some appendix

A.1 ...

Section not in the Table of Contents